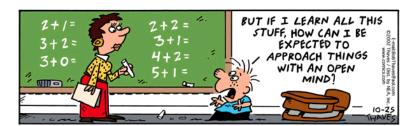
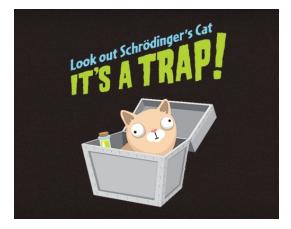
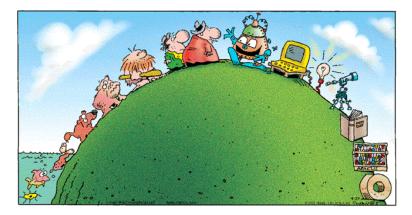


$x^{4} - 8216x^{3} + 25311536x^{2} - 34654562176x + 17790983485440 = 0$









	1	\mathbf{S}	(1803) Guglielmo LIBRI Carucci dalla Sommaja	RM132
			(1878) Agner Krarup ERLANG	
			(1894) Satyendranath BOSE	
•	2	3.5	(1912) Boris GNEDENKO	
1	2	М	(1822) Rudolf Julius Emmanuel CLAUSIUS	
			(1905) Lev Genrichovich SHNIRELMAN	
		-	(1938) Anatoly SAMOILENKO	
	3	T	(1917) Yuri Alexeievich MITROPOLSKY	D3.50 = 1
	4	W	(1643) Isaac NEWTON	RM071
	5	Т	(1838) Marie Ennemond Camille JORDAN	
			(1871) Federigo ENRIQUES	RM084
	_	-	(1871) Gino FANO	
	6	F	(1807) Jozeph Mitza PETZVAL	
	_		(1841) Rudolf STURM	
	7	\mathbf{S}	(1871) Felix Edouard Justin Emile BOREL	
			(1907) Raymond Edward Alan Christopher PALEY	
	8	\mathbf{S}	(1888) Richard COURANT	
			(1924) Paul Moritz COHN	
			(1942) Stephen William HAWKING	
2	9	M	(1864) Vladimir Adreievich STEKLOV	
	10	Т	(1875) Issai SCHUR	
		***	(1905) Ruth MOUFANG	DM100
	11	W	(1545) Guidobaldo DEL MONTE	RM120
			(1707) Vincenzo RICCATI	
	10	m	(1734) Achille Pierre Dionis DU SEJOUR	
	12	Т	(1906) Kurt August HIRSCH	
	13	F	(1864) Wilhelm Karl Werner Otto Fritz Franz WIEN	
			(1876) Luther Pfahler EISENHART	
	14	a	(1876) Erhard SCHMIDT	DMOOR
	14	S	(1902) Alfred TARSKI	RM096
	15	\mathbf{S}	(1704) Johann CASTILLON	
			(1717) Mattew STEWART (1850) Sofia Vasilievna KOVALEVSKAJA	RM144
3	16	М	(1801) Thomas KLAUSEN	10101144
J	16	Т	(1801) Thomas KLAUSEN (1847) Nikolay Egorovich ZUKOWSKY	
	11	T	(1858) Gabriel KOENIGS	
	18	w	(1858) Gabrier KOENIGS (1856) Luigi BIANCHI	
	10	**	(1880) Paul EHRENFEST	
	19	Т	(1880) Faul EINERFEST (1813) Rudolf Friedrich Alfred CLEBSCH	
	13		(1813) Rudon Friedrich Anred CLEBSCH (1879) Guido FUBINI	
			(1908) Aleksandr Gennadievich KUROSH	
	20	F	(1775) André Marie AMPÈRE	
	20	•	(1775) Andre Marie AMI ERE (1895) Gabor SZEGŐ	
			(1993) Gabor SZEGO (1904) Renato CACCIOPPOLI	RM072
	21	\mathbf{S}	(1846) Pieter Hendrik SCHOUTE	1011012
	-1	5	(1915) Yuri Vladimirovich LINNIK	
	22	\mathbf{S}	(1592) Pierre GASSENDI	
		5	(1908) Lev Davidovich LANDAU	RM063
			(1886) John William Navin SULLIVAN	1111000
4	23	М	(1840) Ernst ABBE	
-			(1862) David HILBERT	RM060
	24	Т	(1891) Abram Samoilovitch BESICOVITCH	
		-	(1914) Vladimir Petrovich POTAPOV	
	25	w	(1627) Robert BOYLE	
	_0		(1736) Joseph-Louis LAGRANGE	RM048
			(1843) Karl Hermann Amandus SCHWARZ	
	26	Т	(1799) Benoît Paul Émile CLAPEYRON	
	27	F	(1832) Charles Lutwidge DODGSON	RM108
	28	s	(1701) Charles Marie de LA CONDAMINE	
	-0	5	(1892) Carlo Emilio BONFERRONI	
			(1817) William FERREL	
	29	S		
	29	\mathbf{S}	(1888) Sidney CHAPMAN	
5			(1888) Sidney CHAPMAN (1619) Michelangelo BICCI	
5	30	М	(1619) Michelangelo RICCI	
5				



January

Putnam 1997-A1

A rectangle HOMF has sides HO=11 and OM=5. A triangle ABC has H as the intersection of the altitudes, O the centre of the circumscribed circle, M the midpoint of BC, and F the foot of the altitude from A. What is the length of BC?



Things That Math and Sex Have in Common

Explicit discussions of either topic is a *faux pas* at most cocktail parties.

Mathematic Humour

Mathematics is made of 50 percent formulas, 50 percent proofs, and 50 percent imagination.

"Can you do addition?" the White Queen asked. "What's one and one?" "I don't know," said Alice. "I lost count.".

Charles Lutwidge DODGSON

The art of doing mathematics consists in finding that special case which contains all the germs of generality. David HILBERT

Say what you know, do what you must, come what may. [Motto on her paper "On the Problem of the Rotation of a Solid Body about a Fixed Point."].

Sofia Vasilievna KOVALEVSKAJA

When we ask advice, we are usually looking for an accomplice.

Joseph-Louis LAGRANGE

The mathematician is entirely free, within the limits of his imagination, to construct what worlds he pleases. What he is to imagine is a matter for his own caprice; he is not thereby discovering the fundamental principles of the universe nor becoming acquainted with the ideas of God. If he can find, in experience, sets of entities which obey the same logical scheme as his mathematical entities, then he has applied his mathematics to the external world; he has created a branch of science.

John William Navin SULLIVAN

I have no certainties, at most probabilities.

Renato CACCIOPPOLI

[Poisson's] only passion has been science: he lived and is dead for it.

Guglielmo LIBRI Carucci dalla Sommaja

	1	117	(1000) John Charles BUBKILI	
	1	W	(1900) John Charles BURKILL	
	2	Т	(1522) Lodovico FERRARI	D1050
	3	F	(1893) Gaston Maurice JULIA	RM073
	4	\mathbf{S}	(1905) Eric Cristopher ZEEMAN	
	5	S	(1757) Jean Marie Constant DUHAMEL	
6	6	М	(1465) Scipione DEL FERRO	RM064
			(1612) Antoine ARNAULD	
		_	(1695) Nicolaus (II) BERNOULLI	RM093
	7	Т	(1877) Godfried Harold HARDY	RM049
			(1883) Eric Temple BELL	
	8	W	(1700) Daniel BERNOULLI	RM093
			(1875) Francis Ysidro EDGEWORTH	
			(1928) Ennio DE GIORGI	RM133
	9	Т	(1775) Farkas Wolfgang BOLYAI	
			(1907) Harold Scott MacDonald COXETER	RM097
	10	\mathbf{F}	(1747) AIDA Yasuaki	RM121
	11	\mathbf{S}	(1800) William Henry Fox TALBOT	
			(1839) Josiah Willard GIBBS	
			(1915) Richard Wesley HAMMING	
	12	\mathbf{S}	(1914) Hanna CAEMMERER NEUMANN	
7	13	М	(1805) Johann Peter Gustav LEJEUNE DIRICHLET	RM145
	14	Т	(1468) Johann WERNER	
			(1849) Hermann HANKEL	
			(1896) Edward Artur MILNE	
	15	W	(1564) Galileo GALILEI	RM085
			(1861) Alfred North WHITEHEAD	
		-	(1946) Douglas HOFSTADTER	
	16	Т	(1822) Francis GALTON	
			(1853) Gregorio RICCI-CURBASTRO	
		_	(1903) Beniamino SEGRE	
	17	F	(1890) Sir Ronald Aylmer FISHER	
		~	(1891) Adolf Abraham Halevi FRAENKEL	
	18	\mathbf{S}	(1404) Leon Battista ALBERTI	
		~	(1919) Clifford TRUESDELL	
	19	S	(1473) Nicolaus COPERNICUS	
8	20	Μ	(1844) Ludwig BOLTZMANN	RM061
	21	Т	(1591) Girard DESARGUES	
			(1915) Evgeny Michailovich LIFSHITZ	
	22	W	(1903) Frank Plumpton RAMSEY	
	23	Т	(1583) Jean-Baptiste MORIN	
	<u>.</u>	-	(1951) Shigefumi MORI	
	24	F	(1871) Felix BERNSTEIN	
	25	\mathbf{S}	(1827) Henry WATSON	
	26	\mathbf{S}	(1786) Dominique Francois Jean ARAGO	
9	27	М	(1881) Luitzen Egbertus Jan BROUWER	
	28	Т	(1735) Alexandre Theophile VANDERMONDE	
	29	W	(1860) Herman HOLLERITH	RM109



February

Putnam 1997-A2

Players 1, 2, 3, ..., n are seated around a table, and each has a single penny. Player 1 passes a penny to player 2, who then passes two pennies to player 3. Player 3 then passes one penny to Player 4, who passes two pennies to Player 5, and so on, players alternately passing one penny or two to the next player who still has some pennies. A player who runs out of pennies drops out of the game and leaves the table. Find an infinite set of numbers n for which some player ends up with all npennies.

Things That Math and Sex Have in Common

Historically, men have been in control, but there are now efforts to get women more involved.

Mathematic Humour

"A mathematician is a device for turning coffee into theorems" (P. Erdős)

Addendum: American coffee is good for lemmas.

Euclid taught me that without assumptions there is no proof. Therefore, in any argument, examine the assumptions.

Eric Temple BELL

Mathemata mathematicis scribuntur.

(Mathematics is written for mathematicians). Nicolaus COPERNICUS

A beautiful problem, even if you don't solve it, keeps you company when you think of it from time to time. Ennio DE GIORGI

Natural selection is a mechanism for generating an exceedingly high degree of improbability. Sir Ronald Aylmer FISHER

Measure what is measurable, and make measurable what is not so.

Galileo GALILEI

Mathematics is an interesting intellectual sport but it should not be allowed to stand in the way of obtaining sensible information about physical processes. Richard Wesley HAMMING

Even mathematics is a science done by humans, and so each time, as each nation has its own spirit. Hermann HANKEL

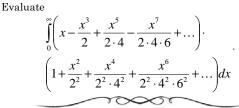
I am interested in mathematics only as a creative art. Godfried Harold HARDY

	-	m		
	1	Т	(1611) John PELL	
	2	F	(1836) Julius WEINGARTEN	
	3	\mathbf{S}	(1838) George William HILL	DISAGO
			(1845) Georg CANTOR	RM062
		c	(1916) Paul Richard HALMOS	
10	4	S	(1822) Jules Antoine LISSAJOUS	
10	5	м	(1512) Gerardus MERCATOR	
			(1759) Benjamin GOMPERTZ	
			(1817) Angelo GENOCCHI (1915) Laurent SOLUMA DEZ	
	c	m	(1915) Laurent SCHWARTZ	
	6	T	(1866) Ettore BORTOLOTTI	DM140
	7	W	(1792) William HERSCHEL (1824) Delfino CODAZZI	RM146
	ø	Т	(1824) Dennio CODAZZI (1851) George CHRYSTAL	
	8 9	F	(1851) George CHRISTAL (1818) Ferdinand JOACHIMSTHAL	
	9	г	(1918) Ferdinand JOACHIMSTHAL (1900) Howard Hathaway AIKEN	
	10	\mathbf{S}	(1960) Howard Hathaway AIKEN (1864) William Fogg OSGOOD	
	10	S	(1804) William Fogg OSGOOD (1811) Urbain Jean Joseph LE VERRIER	
	11	a	(1853) Salvatore PINCHERLE	
11	12	М	(1685) George BERKELEY	
11	14	IVI	(1835) George BERRELET (1824) Gustav Robert KIRCHHOFF	
			(1859) Ernesto CESARO	
	13	т	(1861) Jules Joseph DRACH	
	10	-	(1957) Rudy D'ALEMBERT	
	14	w	(1864) Jozef KURSCHAK	
			(1879) Albert EINSTEIN	RM074
	15	Т	(1860) Walter Frank Raphael WELDON	
			(1868) Grace CHISOLM YOUNG	
	16	F	(1750) Caroline HERSCHEL	RM146
			(1789) Georg Simon OHM	
			(1846) Magnus Gosta MITTAG-LEFFLER	
	17	\mathbf{S}	(1876) Ernest Benjamin ESCLANGON	
			(1897) Charles FOX	
	18	\mathbf{S}	(1640) Philippe de LA HIRE	
			(1690) Christian GOLDBACH	RM122
			(1796) Jacob STEINER	
12	19	М	(1862) Adolf KNESER	
			(1910) Jacob WOLFOWITZ	
	20	Т	(1840) Franz MERTENS	
			(1884) Philip FRANCK (1998) Sauri Betarrich NOVIKOV	
	01	117	(1938) Sergi Petrovich NOVIKOV	
	21	W	(1768) Jean Baptiste Joseph FOURIER (1884) George David BIRKHOFF	
	22	Т	(1884) George David BIRKHOFF (1917) Irving KAPLANSKY	
	$\frac{22}{23}$	т F	(1917) Irving KAPLANSKY (1754) Georg Freiherr von VEGA	
	40	T,	(1754) Georg Freiherr von VEGA (1882) Emmy Amalie NOETHER	RM050
			(1892) Emily Amale NOETHER (1897) John Lighton SYNGE	101000
	24	\mathbf{S}	(1809) Joseph LIOUVILLE	
		~	(1948) Sun-Yung (Alice) CHANG	
			(1966) Gigliola STAFFILANI	RM142
	25	\mathbf{S}	(1538) Christopher CLAUSIUS	
13	26	M	(1848) Konstantin ANDREEV	
			(1913) Paul ERDŐS	RM110
İ	27	Т	(1857) Karl PEARSON	
	28	w	(1749) Pierre-Simon de LAPLACE	
		-	(1928) Alexander GROTHENDIECK	RM086
	29	Т	(1825) Francesco FAA' DI BRUNO	
			(1873) Tullio LEVI-CIVITA	RM098
			(1896) Wilhelm ACKERMAN	
	30	F	(1892) Stefan BANACH	RM134
	31	\mathbf{S}	(1596) René DESCARTES	



March

Putnam 1997-A3



Things That Math and Sex Have in Common

There are many joint results.

Mathematic Humour

Mathematicians are like Frenchmen: whatever you say to them, they translate it into their own language, and forthwith it means something entirely different. (Goethe)

500

The essence of mathematics lies in its freedom.

Georg CANTOR

When writing about transcendental issues, be transcendentally clear. René DESCARTES

I don't believe in mathematics.

```
Albert EINSTEIN
```

Mathematics is not yet ready for such problems. [Attributed by Paul Halmos]

Paul ERDŐS

... the student skit at Christmas contained a plaintive line: "Give us Master's exams that our faculty can pass, or give us a faculty that can pass our Master's exams.". Paul Richard HALMOS

Nature laughs at the difficulties of integration. Pierre-Simon de LAPLACE

The calculus is the greatest aid we have to the application of physical truth in the broadest sense of the word. William Fogg OSGOOD

"The northern ocean is beautiful", said the Orc, "and beautiful the delicate intricacy of the snowflake before it melts and perishes, but such beauties are as nothing to him who delights in numbers, spurning alike the wild irrationality of life and the baffling complexities of nature's laws."

John Lighton SYNGE

	1	\mathbf{S}	(1640) Georg MOHR	
			(1776) Marie-Sophie GERMAIN	
	-		(1895) Alexander Craig AITKEN	
14	2	Μ	(1934) Paul Joseph COHEN	
	3	Т	(1835) John Howard Van AMRINGE	
			(1900) Albert Edward INGHAM	
			(1909) Stanislaw Marcin ULAM	
		***	(1971) Alice RIDDLE	DM100
	4	W	(1809) Benjamin PEIRCE	RM123
			(1842) Francois Edouard Anatole LUCAS (1949) Shing-Tung YAU	
	5	т	(1588) Thomas HOBBES	
	9	1	(1607) Honoré FABRI	
			(1622) Vincenzo VIVIANI	
			(1869) Sergi Alexeievich CHAPLYGIN	
	6	F	(1801) William Hallowes MILLER	
	7	s	(1768) François-Joseph FRANÇAIS	
	8	$\tilde{\mathbf{s}}$	(1903) Marshall Harvey STONE	
15	9	M	(1791) George PEACOCK	
10	Ũ		(1816) Charles Eugene DELAUNAY	
			(1919) John Presper HECKERT	
	10	Т	(1857) Henry Ernest DUDENEY	
	11	W	(1953) Andrew John WILES	
	12	Т	(1794) Germinal Pierre DANDELIN	
			(1852) Carl Louis Ferdinand Von LINDEMANN	
			(1903) Jan TINBERGEN	
	13	\mathbf{F}	(1728) Paolo FRISI	
			(1813) Duncan Farquharson GREGORY	
			(1879) Francesco SEVERI	
	14	\mathbf{S}	(1629) Christiaan HUYGENS	RM135
	15	\mathbf{S}	(1452) Leonardo da VINCI	
			(1548) Pietro Antonio CATALDI	
			(1707) Leonhard EULER	RM051
			(1809) Herman Gunther GRASSMANN	
16	16	М	(1682) John HADLEY	
		m	(1823) Ferdinand Gotthold Max EISENSTEIN	
	17	Т	(1798) Etienne BOBILLIER (1853) Arthur Moritz SCHONFLIES	
			(1863) Augustus Edward Hough LOVE	
	18	w	(1791) Ottaviano Fabrizio MOSSOTTI	RM150
	10	••	(1907) Lars Valerian AHLFORS	1011150
			(1918) Hsien Chung WANG	
			(1949) Charles Louis FEFFERMAN	
	19	Т	(1880) Evgeny Evgenievich SLUTSKY	
			(1883) Richard VON MISES	
			(1901) Kiyoshi OKA	
			(1905) Charles EHRESMANN	
	20	\mathbf{F}	(1839) Francesco SIACCI	
	21	\mathbf{S}	(1652) Michel ROLLE	
			(1774) Jean Baptiste BIOT	
			(1875) Teiji TAKAGI	
	22	\mathbf{S}	(1811) Otto Ludwig HESSE	
			(1887) Harald August BOHR	RM063
17	23	M	(1858) Max Karl Ernst Ludwig PLANCK	
	24	Т	(1863) Giovanni VAILATI	
	~-		(1899) Oscar ZARISKI	RM099
	25	W	(1849) Felix Christian KLEIN	
			(1900) Wolfgang PAULI (1902) Andrei Nischerseich KOLMOCOBOV	
	0.0	A	(1903) Andrei Nicolayevich KOLMOGOROV	
	26	Т	(1889) Ludwig Josef Johan WITTGENSTEIN	
	27	F	(1755) Marc-Antoine PARSEVAL des Chenes	
	90	C	(1932) Gian-Carlo ROTA	DMOOF
	28 20	S	(1906) Kurt GODEL	RM087 PM075
10	29	S M	(1854) Jules Henri POINCARE (1777) Johann Carl Friedrich GAUSS	RM075 RM147
18	30	IVI	(1777) Johann Carl Friedrich GAUSS (1916) Claude Elwood SHANNON	RM147 RM111
				10101111



April

Putnam 1997-A4

Let *G* be a group with identity *e* and $\phi: G \to G$ a function such that:

 $\phi(g_1)\phi(g_2)\phi(g_3) = \phi(h_1)\phi(h_2)\phi(h_3)$

whenever $g_1g_2g_3 = e = h_1h_2h_3$. Prove that there exists an element $a \in G$ such that $\psi(x) = a\phi(x)$ is an homomorphism (i.e. $\psi(xy) = \psi(x)\psi(y) \forall x, y \in G$). 10000

Things That Math and Sex Have in Common

Both are prominent on college campuses, and are usually practiced indoors. TCX DO

Mathematic Humour

A statistician is someone who is good with numbers but lacks the personality to be an accountant. CXXXX

The notion of a set is too vague for the continuum hypothesis to have a positive or negative answer. Paul Joseph COHEN

You know that I write slowly. This is chiefly because I am never satisfied until I have said as much as possible in a few words, and writing briefly takes far more time than writing at length.

Johann Carl Friedrich GAUSS

I don't believe in natural science. [Said to physicist John Bahcalll.

Kurt GODEL

To understand this for sense it is not required that a man should be a geometrician or a logician, but that he should be mad. ["This" is that the volume generated by revolving the region under 1/x from 1 to infinity has finite volume]. Thomas HOBBES

The fact that the author thinks slowly is not serious, but the fact that he publishes faster than he thinks is inexcusable.

Wolfgang PAULI

If anybody says he can think about quantum problems without getting giddy, that only shows he has not understood the first thing about them.

Max Karl Ernst Ludwig PLANCK

The fact that in mathematics you take everything literally makes this discipline so far away from the needs of physicists as the story of the Wizard of Oz could be. Gian-Carlo ROTA

	1	т	(1825) Johann Jacob BALMER	RM122
	2	w	(1860) D'Arcy Wentworth THOMPSON	RM122 RM138
	4	••	(1905) Kazimierz ZARANKIEWITZ	101100
	3	т	(1842) Otto STOLZ	
	0	1	(1860) Vito VOLTERRA	RM136
	4	F	(1845) William Kingdon CLIFFORD	1011150
	5	S	(1833) Lazarus Emmanuel FUCHS	
	0	5	(1897) Francesco Giacomo TRICOMI	
	6	\mathbf{S}	(1872) Willem DE SITTER	
	U	5	(1906) André WEIL	RM088
19	7	М	(1854) Giuseppe VERONESE	101000
10	•		(1881) Ebenezer CUNNINGHAM	
			(1896) Pavel Sergieievich ALEXANDROV	
			(1926) Alexis Claude CLAIRAUT	
	8	Т	(1859) Johan Ludwig William Valdemar JENSEN	
	9	w	(1746) Gaspard MONGE	
			(1876) Gilbert Ames BLISS	
	10	Т	(1788) Augustin Jean FRESNEL	
			(1847) William Karl Joseph KILLING	
			(1958) Piotr Rezierovich SILVERBRAHMS	
	11	F	(1918) Richard Phillips FEYNMAN	RM076
	12	\mathbf{S}	(1820) Florence NIGHTINGALE	RM104
			(1845) Pierre René Jean Baptiste Henry BROCARD	
			(1902) Frank YATES	
	13	\mathbf{S}	(1750) Lorenzo MASCHERONI	
20	14	М	(1832) Rudolf Otto Sigismund LIPSCHITZ	
		_	(1863) John Charles FIELDS	RM100
	15	Т	(1939) Brian HARTLEY	
	16	W	(1718) Maria Gaetana AGNESI	RM112
			(1821) Pafnuti Lvovi CHEBYSHEV	DM100
	17	m	(1911) John (Jack) TODD	RM139
	17 18	T F	(1940) Alan KAY	
	19	г	(1850) Oliver HEAVISIDE (1892) Bertrand Arthur William RUSSELL	RM052
	19	\mathbf{s}	(1919) Georgii Dimitirievich SUVOROV	RM052
	19 20	S	(1919) Georgi Dimutrieven SOVOROV (1861) Henry Seely WHITE	
21	20	M	(1471) Albrecht DÜRER	RM124
41	41	741	(1792) Gustave Gaspard de CORIOLIS	1001124
	22	т	(1792) Gustave Gaspard de Contollis (1865) Alfred Cardew DIXON	
	23	w	(1914) Lipa BERS	RM148
	24 24	Т	(1544) William GILBERT	1011110
	25	F	(1838) Karl Mikailovich PETERSON	
	26	s	(1667) Abraham DE MOIVRE	
		~	(1896) Yuri Dimitrievich SOKOLOV	
	27	\mathbf{S}	(1862) John Edward CAMPBELL	
22	28	M	(1676) Jacopo Francesco RICCATI	
-	-	-	(1710) Johann (II) BERNOULLI	RM093
		Т	(1882) Harry BATEMAN	
	29	1		
	29 30	W	(1814) Eugene Charles CATALAN	



May

Putnam 1997-A5

Let N_n the number of ordered *n*-tuples of positive integers $(a_1, a_2, ..., a_n)$ such that $(1/a_1 + 1/a_2 + ... + 1/a_n) = 1$. Determine whether N_{10} is even or odd.

10001

Things That Math and Sex Have in Common

Most people wish they knew more about both subjects.

Mathematic Humour

Classification of mathematical problems as linear and nonlinear is like classification of the Universe as bananas and non-bananas.

We have a habit in writing articles published in scientific journals to make the work as finished as possible, to cover up all the tracks, to not worry about the blind alleys or describe how you had the wrong idea first, and so on. So there isn't any place to publish, in a dignified manner, what you actually did in order to get to do the work.

Richard Phillips FEYNMAN

For those who want some proof that physicists are human, the proof is in the idiocy of all the different units which they use for measuring energy.

Richard Phillips FEYNMAN

Why should I refuse a good dinner simply because I don't understand the digestive processes involved. [reply when criticised for his daring use of operators before they could be justified formally]

Oliver HEAVISIDE

[Upon hearing via Littlewood an exposition on the theory of relativity:] To think I have spent my life on absolute muck.

Bertrand Arthur William RUSSELL

If mathematics makes people talk of more than mathematics, then it works well. Piotr Rezierovich SILVERBRAHMS

Mathematics is the highest and most precise expression of the truth.

Giuseppe VERONESE

God exists since mathematics is consistent, and the Devil exists since we cannot prove it.

André WEIL

1 22 3 22 4 5 6 7 8 9 10	2 S 3 S 4 M 5 T 6 W 7 T 8 F 9 S	 (1796) Sadi Leonard Nicolas CARNOT (1851) Edward Bailey ELLIOTT (1899) Edward Charles TITCHMARSH (1895) Tibor RADÓ (1659) David GREGORY (1809) John Henry PRATT (1814) Pierre Laurent WANTZEL (1819) John Couch ADAMS (1436) Johann Muller REGIOMONTANUS (1857) Aleksandr Michailovitch LYAPUNOV (1906) Max ZORN (1863) Edward Burr VAN VLECK (1625) Giovanni Domenico CASSINI (1858) Charlotte Angas SCOTT (1860) Alicia Boole STOTT (1885) John Edensor LITTLEWOOD (940) Mohammad ABU'L WAFA Al-Buzjani (1887) Vladimir Ivanovich SMIRNOV 	RM065 RM077 RM049
3 22 4 5 6 7 8 8	3 S 4 M 5 T 6 T 7 T 7 T 7 T 8 F 9 S 9 S 1 M	 (1899) Edward Charles TITCHMARSH (1895) Tibor RADÓ (1659) David GREGORY (1809) John Henry PRATT (1814) Pierre Laurent WANTZEL (1819) John Couch ADAMS (1436) Johann Muller REGIOMONTANUS (1857) Aleksandr Michailovitch LYAPUNOV (1906) Max ZORN (1863) Edward Burr VAN VLECK (1625) Giovanni Domenico CASSINI (1858) Charlotte Angas SCOTT (1860) Alicia Boole STOTT (1885) John Edensor LITTLEWOOD (940) Mohammad ABU'L WAFA Al-Buzjani (1887) Vladimir Ivanovich SMIRNOV 	RM077
3 22 4 5 6 7 8 8	3 S 4 M 5 T 6 T 7 T 7 T 7 T 8 F 9 S 9 S 1 M	(1895) Tibor RADÓ (1659) David GREGORY (1809) John Henry PRATT (1814) Pierre Laurent WANTZEL (1819) John Couch ADAMS (1436) Johann Muller REGIOMONTANUS (1857) Aleksandr Michailovitch LYAPUNOV (1906) Max ZORN (1863) Edward Burr VAN VLECK (1625) Giovanni Domenico CASSINI (1858) Charlotte Angas SCOTT (1860) Alicia Boole STOTT (1885) John Edensor LITTLEWOOD (940) Mohammad ABU'L WAFA Al-Buzjani (1887) Vladimir Ivanovich SMIRNOV	RM077
3 22 4 5 6 7 8 8	3 S 4 M 5 T 6 T 7 T 7 T 7 T 8 F 9 S 9 S 1 M	 (1659) David GREGORY (1809) John Henry PRATT (1814) Pierre Laurent WANTZEL (1819) John Couch ADAMS (1436) Johann Muller REGIOMONTANUS (1857) Aleksandr Michailovitch LYAPUNOV (1906) Max ZORN (1863) Edward Burr VAN VLECK (1625) Giovanni Domenico CASSINI (1858) Charlotte Angas SCOTT (1860) Alicia Boole STOTT (1885) John Edensor LITTLEWOOD (940) Mohammad ABU'L WAFA Al-Buzjani (1887) Vladimir Ivanovich SMIRNOV 	RM077
22 4 5 6 7 8 9	M 5 T 5 W 7 T 7 T 8 F 9 S 0 S 1 M	 (1809) John Henry PRATT (1814) Pierre Laurent WANTZEL (1819) John Couch ADAMS (1436) Johann Muller REGIOMONTANUS (1857) Aleksandr Michailovitch LYAPUNOV (1906) Max ZORN (1863) Edward Burr VAN VLECK (1625) Giovanni Domenico CASSINI (1858) Charlotte Angas SCOTT (1860) Alicia Boole STOTT (1885) John Edensor LITTLEWOOD (940) Mohammad ABU'L WAFA Al-Buzjani (1887) Vladimir Ivanovich SMIRNOV 	RM077
5 6 7 8 9	5 T 5 W 7 T 3 F 0 S 0 S 1 M	 (1814) Pierre Laurent WANTZEL (1819) John Couch ADAMS (1436) Johann Muller REGIOMONTANUS (1857) Aleksandr Michailovitch LYAPUNOV (1906) Max ZORN (1863) Edward Burr VAN VLECK (1625) Giovanni Domenico CASSINI (1858) Charlotte Angas SCOTT (1860) Alicia Boole STOTT (1885) John Edensor LITTLEWOOD (940) Mohammad ABU'L WAFA Al-Buzjani (1887) Vladimir Ivanovich SMIRNOV 	RM077
6 7 8 9	6 W 7 T 3 F 0 S 0 S	(1819) John Couch ADAMS (1436) Johann Muller REGIOMONTANUS (1857) Aleksandr Michailovitch LYAPUNOV (1906) Max ZORN (1863) Edward Burr VAN VLECK (1625) Giovanni Domenico CASSINI (1858) Charlotte Angas SCOTT (1860) Alicia Boole STOTT (1885) John Edensor LITTLEWOOD (940) Mohammad ABU'L WAFA Al-Buzjani (1887) Vladimir Ivanovich SMIRNOV	RM077
7 8 9	7 T 3 F 9 S 0 S 1 M	 (1436) Johann Muller REGIOMONTANUS (1857) Aleksandr Michailovitch LYAPUNOV (1906) Max ZORN (1863) Edward Burr VAN VLECK (1625) Giovanni Domenico CASSINI (1858) Charlotte Angas SCOTT (1860) Alicia Boole STOTT (1885) John Edensor LITTLEWOOD (940) Mohammad ABU'L WAFA Al-Buzjani (1887) Vladimir Ivanovich SMIRNOV 	
7 8 9	7 T 3 F 9 S 0 S 1 M	 (1857) Aleksandr Michailovitch LYAPUNOV (1906) Max ZORN (1863) Edward Burr VAN VLECK (1625) Giovanni Domenico CASSINI (1858) Charlotte Angas SCOTT (1860) Alicia Boole STOTT (1885) John Edensor LITTLEWOOD (940) Mohammad ABU'L WAFA Al-Buzjani (1887) Vladimir Ivanovich SMIRNOV 	
8	B F D S 0 S 1 M	(1906) Max ZORN (1863) Edward Burr VAN VLECK (1625) Giovanni Domenico CASSINI (1858) Charlotte Angas SCOTT (1860) Alicia Boole STOTT (1885) John Edensor LITTLEWOOD (940) Mohammad ABU'L WAFA Al-Buzjani (1887) Vladimir Ivanovich SMIRNOV	
8	B F D S 0 S 1 M	(1863) Edward Burr VAN VLECK (1625) Giovanni Domenico CASSINI (1858) Charlotte Angas SCOTT (1860) Alicia Boole STOTT (1885) John Edensor LITTLEWOOD (940) Mohammad ABU'L WAFA Al-Buzjani (1887) Vladimir Ivanovich SMIRNOV	RM049
8	B F D S 0 S 1 M	 (1625) Giovanni Domenico CASSINI (1858) Charlotte Angas SCOTT (1860) Alicia Boole STOTT (1885) John Edensor LITTLEWOOD (940) Mohammad ABU'L WAFA Al-Buzjani (1887) Vladimir Ivanovich SMIRNOV 	RM049
9) S 0 S 1 M	 (1858) Charlotte Angas SCOTT (1860) Alicia Boole STOTT (1885) John Edensor LITTLEWOOD (940) Mohammad ABU'L WAFA Al-Buzjani (1887) Vladimir Ivanovich SMIRNOV 	RM049
-	0 S	(1860) Alicia Boole STOTT (1885) John Edensor LITTLEWOOD (940) Mohammad ABU'L WAFA Al-Buzjani (1887) Vladimir Ivanovich SMIRNOV	RM049
-	0 S	(1885) John Edensor LITTLEWOOD (940) Mohammad ABU'L WAFA Al-Buzjani (1887) Vladimir Ivanovich SMIRNOV	RM049
-	0 S	(940) Mohammad ABU'L WAFA Al-Buzjani (1887) Vladimir Ivanovich SMIRNOV	RM049
10	1 M	(1887) Vladimir Ivanovich SMIRNOV	
I			DM101
0.0 1			RM101
-	2 T	(1937) David Bryant MUMFORD	
1	0 117	(1888) Zygmunt JANYSZEWSKI	DW110
13	3 W	(1831) James Clerk MAXWELL	RM113
		(1876) William Sealey GOSSET (Student)	DM140
1	4 m	(1928) John Forbes NASH (1736) Charles Augustin de COULOMB	RM149
14	4 T	(1736) Charles Augustin de COULOMB (1856) Andrei Andreyevich MARKOV	DM10F
		(1856) Andrei Andreyevich MARKOV (1903) Alonzo CHURCH	RM125
18	5 F	(1640) Bernard LAMY	
1,	0 I	(1894) Nikolai Gregorievich CHEBOTARYOV	
10	6 S	(1915) John Wilder TUKEY	
1'		(1898) Maurits Cornelius ESCHER	RM097
24 18		(1858) Andrew Russell FORSYTH	1011001
	0 112	(1884) Charles Ernest WEATHERBURN	
		(1913) Paul TEICHMUELLER	RM148
19	9 T	(1623) Blaise PASCAL	RM053
		(1902) Wallace John ECKERT	
20	0 W	(1873) Alfred LOEWY	
2	1 T	(1781) Simeon Denis POISSON	
		(1828) Giuseppe BRUNO	
22	2 F	(1822) Mario PIERI	
		(1864) Hermann MINKOWSKY	
		(1910) Konrad ZUSE	
23	3 S	(1912) Alan Mathison TURING	RM089
24	4 S	(1880) Oswald VEBLEN	
25 24	5 M	(1908) William Van Orman QUINE	
20	6 T	(1823) William THOMSON, Lord Kelvin	
		(1918) Yudell Leo LUKE	
2'	7 W	(1806) Augustus DE MORGAN	
28	8 T	(1875) Henri Leon LEBESGUE	
29	9 F	(1888) Aleksandr Aleksandrovich FRIEDMANN	RM101
30	0 S	(1791) Felix SAVART	



June

Putnam 1997-A6

For a positive integer *n* and any real number *c*, define x_k recursively by $x_0=0$, $x_1=1$, and for $k \ge 0$,

$$x_{k+2} = \frac{cx_{k+1} - (n-k)x_k}{k+1}.$$

Fix *n* and then take *c* to be the largest value for which $x_{n+1}=0$. Find x_k in terms of *n* and *k*, $1 \le k \le n$.

Things That Math and Sex Have in Common

Both can produce interesting topology and geometry.

Mathematic Humour

The difference between an introvert and extrovert mathematicians is: An introvert mathematician looks at his shoes while talking to you. An extrovert mathematician looks at your shoes.

It is easier to square the circle than to get round a mathematician.

Augustus DE MORGAN

Mathematics is the only good metaphysics. William THOMSON, Lord Kelvin

A good mathematical joke is better, and better mathematics, than a dozen mediocre papers. John Edensor LITTLEWOOD

It is possible for a mathematician to be "too strong" for a given occasion. he forces through, where another might be driven to a different, and possible more fruitful, approach. (So a rock climber might force a dreadful crack, instead of finding a subtle and delicate route). John Edensor LITTLEWOOD

... that, in a few years, all great physical constants will have been approximately estimated, and that the only occupation which will be left to men of science will be to carry these measurements to another place of decimals. [Maxwell strongly disagreed with these views and was attacking them].

James Clerk MAXWELL

I think women are biologically better suited to mathematics. The study and application of mathematics does not require any physical strength. A man and a woman can not compete on the tennis court but may do so on a study of numbers, where the only force necessary is mental.

John Forbes NASH

	1	C	(1642) Clatterial Will also and LEIDNIZ	DMOTA
	1	\mathbf{S}	(1643) Gottfried Wilhelm von LEIBNIZ (1788) Jean Victor PONCELET	RM054
26	2	М	(1788) Jean Victor FONCELET (1820) William John Racquorn RANKINE	
20	4	IVI.	(1820) William BURNSIDE	
	3	т	(1807) Ernest Jean Philippe Fauque de	
	3	-	JONQUIERE	
			(1897) Jesse DOUGLAS	
	4	W	(1906) Daniel Edwin RUTHERFORD	
			(1917) Michail Samoilovich LIVSIC	
	5	Т	(1936) James MIRRLEES	
	6	F	(1849) Alfred Bray KEMPE	
	7	\mathbf{S}	(1816) Johann Rudolf WOLF (1906) William FELLER	
			(1906) William FELLER (1922) Vladimir Aleksandrovich MARCHENKO	
	8	\mathbf{S}	(1760) Christian KRAMP	
	Ū	N	(1904) Henri Paul CARTAN	RM126
27	9	М	(1845) George Howard DARWIN	RM138
	10	Т	(1862) Roger COTES	
			(1868) Oliver Dimon KELLOGG	
	11	W	(1857) Sir Joseph LARMOR	
			(1888) Jacob David TAMARKIN	RM101
	12	т	(1890) Giacomo ALBANESE	
	12	1	(1875) Ernest Sigismund FISCHER (1895) Richard BUCKMINSTER FULLER	RM066
			(1935) Nicolas BOURBAKI	RM126
	13	F	(1527) John DEE	
			(1741) Karl Friedrich HINDENBURG	
	14	\mathbf{S}	(1671) Jacques D'ALLONVILLE	
			(1793) George GREEN	RM078
	15	\mathbf{S}	(1865) Wilhelm WIRTINGER	
28	16	М	(1906) Adolph Andrej Pavlovich YUSHKEVICH (1678) Jakob HERMANN	
20	10	IVI	(1903) Irmgard FLUGGE-LOTZ	
	17	Т	(1831) Victor Mayer Amedeè MANNHEIM	
			(1837) Wilhelm LEXIS	
	18	W	(1013) Hermann von REICHENAU	
			(1635) Robert HOOKE	RM114
	19	Т	(1853) Hendrik Antoon LORENTZ	
	19 20	F	(1768) Francois Joseph SERVOIS (1876) Otto BLUMENTHAL	
	20		(1947) Gerd BINNIG	
	21	\mathbf{S}	(1620) Jean PICARD	
			(1848) Emil WEYR	
			(1849) Robert Simpson WOODWARD	
	22	S	(1784) Friedrich Wilhelm BESSEL	
29	23	М	(1775) Etienne Louis MALUS (1854) Ivan SLEZYNSKY	
	24	Т	(1854) Ivan SLEZYNSKY (1851) Friedrich Herman SCHOTTKY	
	44	1	(1851) Friedrich Herman Schol IKI (1871) Paul EPSTEIN	
			(1923) Christine Mary HAMILL	
	25	W	(1808) Johann Benedict LISTING	
	26	Т	(1903) Kurt MAHLER	
	27	\mathbf{F}	(1667) Johann BERNOULLI	RM093
			(1801) George Biddel AIRY	
			(1848) Lorand Baron von EOTVOS	DMOOO
	28	\mathbf{S}	(1871) Ernst Friedrich Ferdinand ZERMELO (1954) Gerd FALTINGS	RM090
	28 29	s S	(1954) Gerd FALTINGS (1898) Isidor Isaac RABI	
30	30	M	(1889) Vladimir Kosma ZWORKYN	
	31	Т	(1704) Gabriel CRAMER	
			(1712) Johann Samuel KOENIG	
			(1926) Hilary PUTNAM	



July

Putnam 1997-B1

Let $\{x\}$ denote the distance between the real number x and the nearest integer. For each positive integer n, evaluate:

 $F_n = \sum_{m=1}^{6n-1} \min\left(\left\{\frac{m}{6n}\right\}, \left\{\frac{m}{3n}\right\}\right).$

Things That Math and Sex Have in Common

Both merit undivided attention, but mathematicians are prone to think about one while doing the other.

Mathematic Humour

Philosophy is a game with objectives and no rules. Mathematics is a game with rules and no objectives.

Everyone is free to think whatever he wants on the nature of mathematical entities, or on the truth of the theorems he uses, under the condition that its reasoning can be written in common language [Zermelo-Fraenkel set theory].

Nicolas BOURBAKI

A marvellous neutrality have these things mathematically, and also a strange participation between things supernaturally, immortally, intellectually, simple and indivisible, and things naturally, mortally, sensible, compounded and divisible.

John DEE

[about him, attributed variously to Charles Louis de Secondat Montesquieu and to the Duchess of Orléans:] It is rare to find learned men who are clean, do not stink and have a sense of humour.

Gottfried Wilhelm von LEIBNIZ

Musica est exercitium arithmeticae occultum nescientis se numerare animi (The pleasure we obtain from music comes from counting, but counting unconsciously. Music is nothing but unconscious arithmetic).

Gottfried Wilhelm von LEIBNIZ

Religion is the mathematics of the poor in spirit. Piergiorgio ODIFREDDI

[The mathematician], asserts only that certain things are possible and others impossible - in a strongly and strictly mathematical sense of "possible" and "impossible".. Hilary PUTNAM

	1	W	(1861) Ivar Otto BENDIXSON	
	0	m	(1881) Otto TOEPLITZ (1856) Ferdinand RUDIO	
	2	Т	(1856) Ferdinand RUDIO (1902) Mina Spiegel REES	
	3	F	(1902) Mina Spieger REES (1914) Mark KAC	RM115
	4	S	(1805) Sir William Rowan HAMILTON	RM079
	T	D	(1838) John VENN	101070
	5	\mathbf{S}	(1802) Niels Henrik ABEL	RM055
			(1941) Alexander Keewatin DEWDNEY	
31	6	Μ	(1638) Nicolas MALEBRANCHE	
			(1741) John WILSON	
	7	Т	(1868) Ladislaus Josephowitsch BORTKIEWITZ	
	8	W	(1902) Paul Adrien Maurice DIRAC	RM103
	-	-	(1931) Sir Roger PENROSE	
	9	Т	(1537) Francesco BAROZZI (Franciscus Barocius)	
	10	F	(1602) Gilles Personne de ROBERVAL	
	11	\mathbf{S}	(1730) Charles BOSSUT (1842) Enrico D'OVIDIO	
	12	\mathbf{s}	(1842) Ellifico D'OVIDIO (1882) Jules Antoine RICHARD	
	14	5	(1887) Erwin Rudolf Josef Alexander	RM103
			SCHRÖDINGER	1001100
32	13	М	(1625) Erasmus BARTHOLIN	
			(1819) George Gabriel STOKES	
			(1861) Cesare BURALI-FORTI	
	14	Т	(1530) Giovanni Battista BENEDETTI	
			(1842) Jean Gaston DARBOUX	
			(1865) Guido CASTELNUOVO (1866) Charles Gustave Nicolas de la VALLÉE-	
			POUSSIN	
	15	w	(1863) Aleksei Nikolaevich KRYLOV	
			(1892) Louis Pierre Victor duc de BROGLIE	
			(1901) Piotr Sergeevich NOVIKOV	
	16	Т	(1773) Louis-Benjamin FRANCOEUR	
			(1821) Arthur CAYLEY	
	17	F	(1601) Pierre de FERMAT	RM091
	18	S	(1685) Brook TAYLOR	
	19	\mathbf{S}	(1646) John FLAMSTEED	
33	20	М	(1739) Georg Simon KLUGEL (1710) Thomas SIMPSON	
00	20	IVI	(1710) Thomas Shirt SON (1863) Corrado SEGRE	
			(1882) Wacłav SIERPIŃSKI	
	21	Т	(1789) Augustin Louis CAUCHY	RM127
	22	w	(1647) Denis PAPIN	
	23	Т	(1683) Giovanni POLENI	
			(1829) Moritz Benedikt CANTOR	
			(1842) Osborne REYNOLDS	
	24	F	(1561) Bartholomeo PITISCUS	
		~	(1942) Karen Keskulla UHLENBECK	
	25	\mathbf{S}	(1561) Philip van LANSBERGE	
	96	ę	(1844) Thomas MUIR (1728) Johann Heinrich LAMBERT	
	26	\mathbf{S}	(1728) Johann Heinrich LAMBERT (1875) Giuseppe VITALI	
			(1975) Gluseppe VITALI (1965) Marcus Peter Francis du SAUTOY	
34	27	М	(1858) Giuseppe PEANO	RM067
	28	Т	(1796) Irénée Jules BIENAYMÉ	
	29	w	(1904) Leonard ROTH	
	30	Т	(1856) Carle David Tolmé RUNGE	
			(1906) Olga TAUSSKY-TODD	RM139
	31	F	(1821) Hermann Ludwig Ferdinand von	
			HELMHOLTZ	



August

Putnam 1997-B2

Let f be a twice-differentiable real-valued function satisfying:

$$f(x) + f''(x) = -xg(x)f'(x),$$

where $g(x) \ge 0$ $\forall x \in R$. Prove that |f(x)| is bounded.

Things That Math and Sex Have in Common

Saint Augustine was hostile to both, and Alan Turing took an unusual approach to both.

Mathematic Humour

What is a *rigorous* definition of rigor?

Divergent series are the invention of the devil. Niels Henrik ABEL

Men pass away, but their deeds abide. [His last words (?)] Augustin Louis CAUCHY

Projective geometry is all geometry.

Arthur CAYLEY

The main activity of mathematical research is to hunt for new theorems.

Alexander Keewatin DEWDNEY

If you ever need to exaggerate a statement, you could always say: "Public spending is growing faster than the Ackermann function".

Alexander Keewatin DEWDNEY

In science one tries to tell people, in such a way as to be understood by everyone, something that no one ever knew before. But in poetry, it's the exact opposite.

Paul Adrien Maurice DIRAC

The essential point of our tradition and our mathematics education is that we should never bow to the authority of some obscure rule that we can never hope to understand. We must see - at least in principle - that every step in a reasoning can be reduced to something simple and obvious. The mathematical truth is not a horribly complicated dogma whose validity is not subject to our understanding: it is built with simple and obvious ingredients, and once we understood them, their truth is clear and is accepted by all.

Sir Roger PENROSE

	1	R	(1650) Level CALIDIN	
	1	\mathbf{S}	(1659) Joseph SAURIN (1835) William Stankey JEVONS	
	2	\mathbf{S}	(1855) William Stankey SEVONS (1878) Mauriche René FRECHET	
	4	3	(1923) René THOM	RM080
35	3	М	(1814) James Joseph SYLVESTER	RM104
00	0		(1884) Solomon LEFSCHETZ	1011104
			(1908) Lev Semenovich PONTRYAGIN	
	4	Т	(1809) Luigi Federico MENABREA	RM150
	5	w	(1667) Giovanni Girolamo SACCHERI	RM128
			(1725) Jean Etienne MONTUCLA	
	6	Т	(1859) Boris Jakovlevich BUKREEV	
			(1863) Dimitri Aleksandrovich GRAVE	
	7	\mathbf{F}	(1707) George Louis Leclerc comte de BUFFON	
			(1955) Efim ZELMANOV	
	8	\mathbf{S}	(1584) Gregorius SAINT-VINCENT	
			(1588) Marin MERSENNE	RM092
	9	\mathbf{S}	(1860) Frank MORLEY	
36	10	М	(1839) Charles Sanders PEIRCE	RM123
	11	Т	(1623) Stefano degli ANGELI	
			(1877) sir James Hopwood JEANS	
	12	W	(1891) Antoine André Louis REYNAUD	
	10	m	(1900) Haskell Brooks CURRY	
	13	Т	(1873) Constantin CARATHÉODORY	
	14	Б	(1885) Wilhelm Johann Eugen BLASCHKE (1858) Henry Burchard FINE	
	14	F	(1858) Henry Burchard FINE (1891) Ivan Matveevich VINOGRADOV	
	15	\mathbf{S}	(973) Abu Arrayhan Muhammad ibn Ahmad	
	10	5	AL'BIRUNI	
			(1886) Paul Pierre LEVY	
	16	\mathbf{S}	(1494) Francisco MAUROLICO	
			(1736) Johann Nikolaus TETENS	
37	17	Μ	(1743) Marie Jean Antoine Nicolas de Caritat de	
			CONDORCET	
			(1826) Georg Friedrich Bernhard RIEMANN	RM068
	18	Т	(1752) Adrien Marie LEGENDRE	RM140
	19	W	(1749) Jean Baptiste DELAMBRE	
	20	Т	(1842) Alexander Wilhelm von BRILL	
	01	Б	(1861) Frank Nelson COLE	
	21 22	F S	(1899) Juliusz Pawel SCHAUDER (1765) Paolo RUFFINI	DM11(
	44	5	(1765) Fablo KOFFINI (1769) Louis PUISSANT	RM116
			(1703) Louis FOISSANT (1803) Jaques Charles Francois STURM	
	23	\mathbf{S}	(1768) William WALLACE	
	20	D	(1900) David van DANTZIG	
38	24	М	(1501) Girolamo CARDANO	RM064
	-	-	(1625) Johan DE WITT	
			(1801) Michail Vasilevich OSTROGRADSKI	RM056
			(1945) Ian Nicholas STEWART	
	25	Т	(1819) George SALMON	
			(1888) Stefan MAZURKIEWICZ	
	26	W	(1688) Willem Jakob 's GRAVESANDE	
			(1854) Percy Alexander MACMAHON	
	a -	m	(1891) Hans REICHENBACH	
	27	Т	(1855) Paul Émile APPELL (1876) Faula Bauman d HEDBICK	
			(1876) Earle Raymond HEDRICK	
	90	F	(1919) James Hardy WILKINSON (1698) Pierre Louis Moreau de MAUPERTUIS	DM1F6
	28	Г	(1698) Pierre Louis Moreau de MAUPERTUIS (1761) Ferdinand Francois Desirè Budan de	RM152
			BOISLAURENT	
			(1873) Julian Lowell COOLIDGE	
	29	\mathbf{S}	(1561) Adriaan van ROOMEN	
	-		(1812) Adolph GOPEL	
	30	\mathbf{S}	(1775) Robert ADRAIN	
			(1829) Joseph WOLSTENHOLME	
			(10_0) occepti (Collectionic)	



September

Putnam 1997-B3

For each positive integer n, write the sum

$$\sum_{n=1}^{n} \frac{1}{m},$$

in the form $rac{p_n}{q_n}$, where p_n and q_n are relatively prime

positive integers. Determine all n such that 5 does not divide q_n .

Things That Math and Sex Have in Common

Both typically begin with a lot of hard work and end with a great but brief reward.

Mathematic Humour

What is the difference between a Psychotic, a Neurotic and a mathematician? A Psychotic believes that 2+2=10. A Neurotic knows that 2+2=4, but it kills him. A mathematician simply changes the base.

From the intrinsic evidence of his creation, the Great Architect of the Universe now begins to appear as a pure mathematician.

sir James Hopwood JEANS

His theorems were always correct: his demonstrations, never." [Said by Gian-Carlo Rota].

Solomon LEFSCHETZ

A moment of drowsiness and old errors are propagated, and new ones are introduced.

Francisco MAUROLICO

The one [the logician] studies the science of drawing conclusions, the other [the mathematician] the science which draws necessary conclusions.

Charles Sanders PEIRCE

Tools of the trade of the mathematician are pencil and paper: as a consequence, no mathematician will bring them with him, and should always borrow a pen and write on a napkin.

Ian Nicholas STEWART

(...) as Brindley, the engineer, once allowed before a parliamentary committee that, in his opinion, rivers were made to feed navigable canals, I feel almost tempted to say that one principal reason for the existence of space, or at least one principal function which it discharges, is that of feeding mathematical invention.

James Joseph SYLVESTER

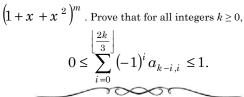
39	1	М	(1671) Luigi Guido GRANDI	
			(1898) Bela KEREKJARTO'	
	2	Т	(1825) John James WALKER	
			(1908) Arthur ERDÉLYI	
	3	W	(1944) Pierre René DELIGNE	
	4	Т	(1759) Louis Francois Antoine ARBOGAST	
	-	17	(1797) Jerome SAVARY	
	5	F	(1732) Nevil MASKELYNE	DM117
			(1781) Bernhard Placidus Johann Nepomuk BOLZANO	RM117
			(1861) Thomas Little HEATH	
	6	\mathbf{S}	(1552) Matteo RICCI	RM141
	U	Б	(1832) Matteo Mileon (1831) Julius Wilhelm Richard DEDEKIND	RM081
			(1908) Sergei Lvovich SOBOLEV	1010001
	7	\mathbf{S}	(1885) Niels BOHR	RM063
40	8	M	(1908) Hans Arnold HEILBRONN	101000
10	9	Т	(1581) Claude Gaspard BACHET de Meziriac	
	U	-	(1704) Johann Andrea von SEGNER	
			(1873) Karl SCHWARZSCHILD	RM153
			(1949) Fan Rong K Chung GRAHAM	RM110
ĺ	10	W	(1861) Heinrich Friedrich Karl Ludwig	
			BURKHARDT	
	11	Т	(1675) Samuel CLARKE	
			(1777) Barnabè BRISSON	
			(1885) Alfred HAAR	
			(1910) Cahit ARF	
	12	\mathbf{F}	(1860) Elmer SPERRY	
	13	\mathbf{S}	(1890) Georg FEIGL	
			(1893) Kurt Werner Friedrich REIDEMEISTER	
		~	(1932) John Griggs THOMSON	
	14	\mathbf{S}	(1687) Robert SIMSON	
			(1801) Joseph Antoine Ferdinand PLATEAU (1868) Alessandro PADOA	
41	15	М	(1608) Evangelista TORRICELLI	
41	19	IVI	(1735) Jesse RAMSDEN	
			(1776) Peter BARLOW	
	16	Т	(1879) Philip Edward Bertrand JOURDAIN	
	17	Ŵ	(1759) Jacob (II) BERNOULLI	RM093
		••	(1888) Paul Isaac BERNAYS	1111000
	18	Т	(1741) John WILSON	
Ì	19	\mathbf{F}	(1903) Jean Frédéric Auguste DELSARTE	
			(1910) Subrahmanyan CHANDRASEKHAR	RM153
	20	\mathbf{S}	(1632) Sir Christopher WREN	RM105
			(1863) William Henry YOUNG	
			(1865) Aleksandr Petrovich KOTELNIKOV	
	21	\mathbf{S}	(1677) Nicolaus (I) BERNOULLI	RM093
			(1823) Enrico BETTI	RM150
			(1855) Giovan Battista GUCCIA	RM129
	0.0	37	(1914) Martin GARDNER	RM137
42	22	М	(1587) Joachim JUNGIUS	
			(1895) Rolf Herman NEVANLINNA	
	<u>.</u>	т	(1907) Sarvadaman CHOWLA (1865) Piers BOHL	
	$\begin{array}{c} 23\\24 \end{array}$	T W	(1865) Piers BOHL (1804) Wilhelm Eduard WEBER	
	24	vv	(1804) Whitein Eduard WEBER (1873) Edmund Taylor WHITTAKER	
	25	Т	(1811) Évariste GALOIS	RM069
	25 26	F	(1849) Ferdinand Georg FROBENIUS	10101003
	20	T.	(1857) Charles Max MASON	
			(1911) Shiing-Shen CHERN	
1	27	\mathbf{S}	(1678) Pierre Remond de MONTMORT	
			(1856) Ernest William HOBSON	
Ì	28	\mathbf{S}	(1804) Pierre François VERHULST	
43	29	M	(1925) Klaus ROTH	
İ	30	Т	(1906) Andrej Nikolaevich TICHONOV	
ĺ	31	W	(1815) Karl Theodor Wilhelm WEIERSTRASS	RM057
			(1935) Ronald Lewis GRAHAM	RM110
-				



October

Putnam 1997-B4

Let $a_{m,n}$ denote the coefficient of x^n in the expansion of



Things That Math and Sex Have in Common

Professionals are generally viewed with suspicion, and most do not earn high pay.

Mathematic Humour

This is a one line proof... if we start sufficiently far to the left...

Speaking of arithmetic (algebra, analysis) as a part of the logic, I imply that I consider the number concept entirely independent of the notions or intuitions of space and time, that I consider it a direct result of the laws of thought. Julius Wilhelm Richard DEDEKIND

Mathematics is not only real, but it is the only reality. That is that entire universe is made of matter, obviously. And matter is made of particles. It's made of electrons and neutrons and protons. So the entire universe is made out of particles. Now what are the particles made out of? They're not made out of anything. The only thing you can say about the reality of an electron is to cite its mathematical properties. So there's a sense in which matter has completely dissolved and what is left is just a mathematical structure.

Martin GARDNER

It would be very discouraging if somewhere down the line you could ask a computer if the Riemann hypothesis is correct and it said, "Yes, it is true, but you won't be able to understand the proof.".

Ronald Lewis GRAHAM

Ptolemy the First once asked Euclid whether there was any shorter way to a knowledge of geometry than by study of The Elements, whereupon Euclid answered that there was no royal road to geometry.

Thomas Little HEATH

I urge to study mathematics also who is preparing to become a lawyer or economist, philosopher and writer ... for I believe and hope that it will not be useless to reason well and clearly express oneself.

Alessandro PADOA

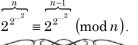
	1	m	(1525) Circulattists DELLA DODTA	
	1	Т	(1535) Giambattista DELLA PORTA	DM004
	2	F	(1815) George BOOLE	RM094
	3	\mathbf{S}	(1867) Martin Wilhelm KUTTA	
			(1878) Arthur Byron COBLE	
		a	(1906) Carl Benjamin BOYER	D 1000
	4	\mathbf{S}	(1744) Johann (III) BERNOULLI	RM093
			(1865) Pierre Simon GIRARD	
44	5	М	(1848) James Whitbread Lee GLAISHER	
		-	(1930) John Frank ADAMS	
	6	Т	(1781) Giovanni Antonio Amedeo PLANA	RM154
	7	W	(1660) Thomas Fantet DE LAGNY	
			(1799) Karl Heinrich GRAFFE	
		_	(1898) Raphael SALEM	
	8	Т	(1656) Edmond HALLEY	
			(1846) Eugenio BERTINI	
			(1848) Fredrich Ludwig Gottlob FREGE	
		-	(1869) Felix HAUSDORFF	
	9	F	(1847) Carlo Alberto CASTIGLIANO	
			(1885) Hermann Klaus Hugo WEYL	RM082
			(1906) Jaroslav Borisovich LOPATYNSKY	
	10	c	(1922) Imre LAKATOS	
	10	S	(1829) Helwin Bruno CHRISTOFFEL	
L	11	S	(1904) John Henry Constantine WHITEHEAD	
45	12	М	(1825) Michail Egorovich VASHCHENKO-	
			ZAKHARCHENKO	
			(1842) John William STRUTT Lord RAYLEIGH	
	10	m	(1927) Yutaka TANIYAMA	
	13	Т	(1876) Ernest Julius WILKZYNSKY	
	14	117	(1878) Max Wilhelm DEHN	
	14	W	(1845) Ulisse DINI	
	15	Т	(1688) Louis Bertrand CASTEL	
			(1793) Michel CHASLES	
	16	F	(1794) Franz Adolph TAURINUS (1835) Eugenio BELTRAMI	RM150
	17	г S	(1597) Henry GELLIBRAND	1111100
	17	э	(1717) Jean Le Rond D'ALEMBERT	
			(1790) August Ferdinand MÖBIUS	RM118
	18	\mathbf{S}	(1872) Giovanni Enrico Eugenio VACCA	1011110
	10	5	(1927) Jon Leslie BRITTON	
46	19	М	(1894) Heinz HOPF	
40	10	MI	(1900) Michail Alekseevich LAVRENTEV	
			(1900) Milenan Alexseevich LAVINEVIEV (1901) Nina Karlovna BARI	
ł	20	т	(1889) Edwin Powell HUBBLE	
	-0	•	(1924) Benoît MANDELBROT	
	21	w	(1867) Dimitri SINTSOV	
	22	т	(1803) Giusto BELLAVITIS	
		•	(1805) Chusto DELLAVITIS (1840) Émile Michel Hyacinthe LEMOINE	
İ	23	F	(1616) John WALLIS	RM070
	-0	-	(1820) Issac TODHUNTER	101/10/10
			(1917) Elizabeth Leonard SCOTT	RM106
İ	24	\mathbf{S}	(1549) Duncan MacLaren Young SOMMERVILLE	
		~	(1909) Gerhard GENTZEN	
İ	25	\mathbf{S}	(1841) Fredrich Wilhelm Karl Ernst SCHRÖDER	
			(1873) Claude Louis MATHIEU	
47	26	М	(1894) Norbert WIENER	
	-		(1946) Enrico BOMBIERI	
İ	27	Т	(1867) Arthur Lee DIXON	
l	<u>-</u> . 28	Ŵ	(1898) John WISHART	
l	29	Т	(1803) Christian Andreas DOPPLER	
		-	(1849) Horace LAMB	
			(1879) Nikolay Mitrofanovich KRYLOV	
İ	30	F	(1549) Sir Henry SAVILE	
		-	(1969) Matilde MARCOLLI	RM142
L				



November

Putnam 1997-B5

Prove that for $n \ge 2$,



Things That Math and Sex Have in Common

Sometimes something useful comes out of it, but that is not the reason we are doing it.

Mathematic Humour

Yeah, I used to think it was just recreational... then I started doin' it during the week... you know, simple stuff: differentiation, kinematics. Then I got into integration by parts... I started doin' it every night: path integrals, holomorphic functions. Now I'm on diophantine equations and sinking deeper into transfinite analysis. Don't let them tell you it's just recreational. Fortunately, I can quit any time I want.

When things get too complicated, it sometimes makes sense to stop and wonder: Have I asked the right question?

Enrico BOMBIERI

Allez en avant, et la foi vous viendra.

Push on and faith will catch up with you. [advice to those who questioned the calculus].

Jean Le Rond D'ALEMBERT

Mathematics is the only instructional material that can be presented in an entirely undogmatic way. Max Wilhelm DEHN

he only reason to believe in mathematic is that mathematic works.

Imre LAKATOS

[responding to Thomas Hobbes, who complained of a page "so covered with crusts of symbols that I did not have the patience to examine if it is proved right or wrong"] Would not it be legal for me to write symbols, until you can understand them? Lord, they are not written for you to read them, but for those who are able to do so.

John WALLIS

My work has always tried to unite the true with the beautiful and when I had to choose one or the other, I usually chose the beautiful.

Hermann Klaus Hugo WEYL

	1	s	(1792) Nikolay Yvanovich LOBACHEVSKY	RM08
	2	$\tilde{\mathbf{s}}$	(1831) Paul David Gustav DU BOIS-REYMOND	101000
	-	0	(1901) George Frederick James TEMPLE	
48	3	М	(1903) Sidney GOLDSTEIN	
10	0		(1924) John BACKUS	
	4	Т	(1795) Thomas CARLYLE	
	5	w	(1868) Arnold Johannes Wilhelm SOMMERFELD	
	0	••	(1900) Werner Karl HEISENBERG	RM15
			(1907) Giuseppe OCCHIALINI	RM12
	6	Т	(1682) Giulio Carlo FAGNANO dei Toschi	1010112
	7	F	(1647) Giovanni CEVA	
	'	T.	(1823) Leopold KRONECKER	
			(1830) Antonio Luigi Gaudenzio Giuseppe	RM15
			CREMONA	101110
	8	\mathbf{S}	(1508) Regnier GEMMA FRISIUS	
	0	0	(1865) Jaques Salomon HADAMARD	
			(1919) Julia Bowman ROBINSON	
	9	\mathbf{S}	(1883) Nikolai Nikolaievich LUZIN	
	Ū	0	(1906) Grace Brewster MURRAY HOPPER	
			(1917) Sergei Vasilovich FOMIN	
49	10	М	(1804) Karl Gustav Jacob JACOBI	
	-•		(1815) Augusta Ada KING Countess of LOVELACE	RM05
	11	Т	(1882) Max BORN	RM15
	12	W	(1832) Peter Ludwig Mejdell SYLOW	
	13	Т	(1724) Franz Ulrich Theodosius AEPINUS	
			(1887) George POLYA	RM13
	14	F	(1546) Tycho BRAHE	
	15	\mathbf{S}	(1802) János BOLYAI	RM08
	16	\mathbf{S}	(1804) Wiktor Yakovievich BUNYAKOWSKY	
50	17	Μ	(1706) Gabrielle Emile Le Tonnelier de Breteuil du	
			CHATELET	
			(1835) Felice CASORATI	
			(1842) Marius Sophus LIE	
			(1900) Dame Mary Lucy CARTWRIGHT	
	18	Т	(1917) Roger LYNDON	
	19	W	(1783) Charles Julien BRIANCHON	
			(1854) Marcel Louis BRILLOUIN	
			(1887) Charles Galton DARWIN	RM13
	20	Т	(1494) Oronce FINE	
			(1648) Tommaso CEVA	
			(1875) Francesco Paolo CANTELLI	
	21	F	(1878) Jan ŁUKASIEWICZ	
			(1932) John Robert RINGROSE	
	22	\mathbf{S}	(1824) Francesco BRIOSCHI	RM15
			(1859) Otto Ludwig HOLDER	
			(1877) Tommaso BOGGIO	
		<i>_</i> .	(1887) Srinivasa Aiyangar RAMANUJAN	
	23	S	(1872) Georgii Yurii PFEIFFER	
51	24	М	(1822) Charles HERMITE	RM09
			(1868) Emmanuel LASKER	
	25	Т	(1642) Isaac NEWTON	RM07
			(1900) Antoni ZYGMUND	
	26	W	(1780) Mary Fairfax Greig SOMERVILLE	D7.5-
			(1791) Charles BABBAGE	RM05
	c -	Ŧ	(1937) John Horton CONWAY	RM11
	27	Т	(1571) Johannes KEPLER	DMAG
		Б	(1654) Jacob (Jacques) BERNOULLI	RM09
	28	F	(1808) Athanase Louis Victoire DUPRÈ	
			(1882) Arthur Stanley EDDINGTON	D3 (1 ^
	00	~	(1903) John von NEUMANN	RM10
	29	S	(1856) Thomas Jan STIELTJES	
	30	S	(1897) Stanislaw SAKS	
52	31	М	(1872) Volodymyr LEVITSKY (1800) Cord Loderin SIECEL	
			(1896) Carl Ludwig SIEGEL (1945) Leonard ADLEMAN	RM14
			(1949) Leonard ADDENNIN (1952) Vaughan Frederick Randall JONES	1010111



December

Putnam 1997-B6

The diameter of a dissection is the least upper bound of the distances between pairs of points belonging to the same part. The dissection of the 3-4-5 triangle in four congruent right triangles similar to the original has diameter 5/2. Find the least diameter of a dissection of this triangle into four parts.

Things That Math and Sex Have in Common

Half the times you get an odd result.

Mathematic Humour

The highest moments in the life of a mathematician are the first few moments after one has proved the result, but before one finds the mistake.

10000

Errors using inadequate data are much less than those using no data at all.

Charles BABBAGE

It is a mathematical fact that the casting of this pebble from my hand alters the centre of gravity of the universe. Thomas CARLYLE

There is one thing the non-mathematicians do not realize, is that mathematics is actually almost entirely an aesthetic subject.

John Horton CONWAY

Each new piece of knowledge is mathematical in form, because we have no other guide possible. Charles Galton DARWIN

Proof is the idol before whom the pure mathematician tortures himself.

Arthur Stanley EDDINGTON

Die ganzen Zahlen hat der liebe Gott gemacht, alles andere ist Menschenwerk.

(God made the integers, all else is the work of man). Leopold KRONECKER

Hypotheses non fingo. (I feign no hypotheses).

Isaac NEWTON

[Her Job Description:] Monday: Try to prove theorem, Tuesday: Try to prove theorem, Wednesday: Try to prove theorem, Thursday: Try to prove theorem, Friday: Theorem false.

Julia Bowman ROBINSON